

ADVERSE SELECTION CLASS PROBLEM

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The Government Employee Car Krash Organization (also known as “GECKO”) does business in Estonia, where automobile liability insurance is not compulsory; i.e., licensed drivers are allowed to (as a matter of their own volition) decide whether or not to purchase such insurance. However, the Estonian insurance commissioner requires that GECKO must offer full coverage and charge the same premium to all of its policyholders. Furthermore, the premium must be set such that the dollar value of GECKO’s expected profit from selling insurance is equal to \$0.

GECKO estimates that the accident probabilities for the following five driver types are as follows (for simplicity, assume that there is only one of each driver type):

Driver Type	Probability of Accident
Cautious Caroline	5%
Nervous Nora	25%
Average Arvis	30%
Aggressive Anna	35%
Hot Rod Henriks	40%

The dollar value of initial wealth and loss due to an accident for all driver types are \$100,000 and \$40,000 respectively. This implies that if an accident occurs, then the dollar value of uninsured wealth falls to \$60,000. Furthermore, utility $U = W^{0.5}$ for all driver types. All drivers can pay the same insurance premium (P) which will fully cover accident-related loss.

1. Suppose that GECKO initially sets the premium at $P = \$10,800$. This premium will enable GECKO to comply with Estonian insurance regulations, so long as all five driver types purchase insurance. Calculate 1) the cross-subsidies that are implied by such a pricing scheme if all five driver types purchase coverage, and 2) expected utilities for all five driver types.
2. Note that Cautious Caroline has higher expected utility if she opts out of purchasing coverage for a price of \$10,800. Since the expected loss costs for the remaining four clients now total \$52,000, the new combined premium will be $\$52,000/4 = \$13,000$. Calculate 1) the cross-subsidies that are implied by such a pricing scheme if the four remaining driver types purchase coverage, and 2) expected utilities for the four remaining driver types.
3. Note that Nervous Nora now has higher expected utility if she opts out of purchasing coverage for a price of \$13,000. Since the expected loss costs for the remaining three clients now total \$42,000, the new combined premium will be $\$42,000/3 = \$14,000$. Calculate 1) the cross-subsidies that are implied by such a pricing scheme if the three remaining driver types purchase coverage, and 2) expected utilities for the three remaining driver types.
4. Since Average Arvis now has higher expected utility if he opts out of purchasing coverage for a price of \$14,000, this leaves only Aggressive Anna and Hot Rod Henriks in the risk pool. Since expected claims costs now total \$30,000, the new combined premium will be $\$30,000/2 = \$15,000$. Calculate 1) the cross-subsidies that are implied by such a pricing scheme if the two remaining driver types purchase coverage, and 2) expected utilities for the two remaining driver types.